Week 5, Day 5
Algebra (2)

Each day covers one maths topic. It should take you about 1 hour or just a little more.

1. Start by reading through the Learning Reminders. They come from our PowerPoint slides.

2. Tackle the questions on the Practice Sheet. There might be a choice of either Mild (easier) or Hot (harder)!
Check the answers.

3. Finding it tricky? That’s OK... have a go with a grown-up at A Bit Stuck?

4. Think you’ve cracked it? Whizzed through the Practice Sheets? Have a go at the Investigation...
Learning Reminders

Make generalisations; Understand and use simple formulae.

This machine does two things, one after the other, to each input.

Someone has tested some inputs and outputs. Look at them and see if you can work out what the machine is doing...
Learning Reminders

Make generalisations; Understand and use simple formulae.

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Learning Reminders

Make generalisations; Understand and use simple formulae.

Function machine rules

- The first function machine: $\times 2, + 1$. If $n$ is the input, the number we put into the machine, we can write the output as $2n + 1$, which means we double the input, then add 1.

- The second function machine: $\times 10, - 1$. If $n$ is the input, we can write the output as $10n - 1$. 
Practice Sheet Mild

Function machines

Work out what each function machine does. Write the output when \( n \) is the input.

\[
\begin{array}{c}
3 \\
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\end{array}
\rightarrow
\begin{array}{c}
15 \\
30 \\
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\[
\begin{array}{c}
10 \\
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\end{array}
\rightarrow
\begin{array}{c}
8 \\
13 \\
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\]

\[
\begin{array}{c}
2 \\
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\end{array}
\rightarrow
\begin{array}{c}
21 \\
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\end{array}
\]

\[
\begin{array}{c}
10 \\
5 \\
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\text{\underline{n}} \\
\end{array}
\rightarrow
\begin{array}{c}
19 \\
9 \\
7 \\
\end{array}
\]

Explore more Hamilton Trust Learning Materials at https://wrht.org.uk/hamilton
Practice Sheet Hot
Function machines

Work out what each function machine does. Write the output when \( n \) is the input.

\[
\begin{align*}
6 &\rightarrow 11 & \quad 6 &\rightarrow 65 \\
15 &\rightarrow 29 & \quad 5 &\rightarrow 55 \\
8 &\rightarrow 15 & \quad 10 &\rightarrow 105 \\
n &\quad & \quad n &
\end{align*}
\]

\[
\begin{align*}
5 &\rightarrow 16 & \quad 10 &\rightarrow 6 \\
10 &\rightarrow 31 & \quad 20 &\rightarrow 11 \\
7 &\rightarrow 22 & \quad 12 &\rightarrow 7 \\
n &\quad & \quad n &
\end{align*}
\]

Challenge
Create your own two step function machine. Choose 3 inputs and find their outputs, swap with a partner. Can you discover each other’s secret function?
Function machines (mild)

3 × 5 = 15  
6 × 5 = 30  
7 × 5 = 35  
5n  
20 + 1 = 21  
4 × 10 + 1 = 41  
10 × 10 + 1 = 101  
10n + 1  

10 - 2 = 8  
15 - 2 = 13  
7 - 2 = 5  
n - 2  
10 - 1 + 10 = 19  
5 - 1 + 5 = 9  
4 - 1 + 4 = 7  
2n - 1  

Function machines (hot)

6 - 1 + 6 = 11  
15 - 1 + 15 = 29  
8 - 1 + 8 = 15  
2n - 1  
5 × 3 + 1 = 16  
10 × 3 + 1 = 31  
7 × 3 + 1 = 22  
3n + 1  
10 + 2 + 1 = 6  
20 + 2 + 1 = 11  
12 + 2 + 1 = 7  
n + 2 + 1
A Bit Stuck?
Function detectives

Look at the inputs and outputs. What calculation(s) is each machine doing?

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S-t-r-e-t-c-h:
Can you write a formula for each machine where n is the input?
Investigation
Stars and crosses

1. Ring a number on the 1-100 grid that is not in a row or column on the edge of the square.
2. Ring the number below, the number above, the number to the left and the number to the right to form a cross.
3. Find the total of the five numbers and make a record of this along with the central number of the cross.
4. Repeat elsewhere on the grid. Can you see a relationship between the central number and the sum of the five numbers in the cross?
5. Why do you think that this relationship holds? Write a formula for finding the total of the five numbers in any cross laid out like this.
6. Now ring numbers in a bigger cross with nine, thirteen or even more numbers! See if you can predict the total. You may want to use a calculator to speed up the process if your cross is really big.

Can you write formula for finding the total of ANY cross that will fit on the grid?

What if this was not a 1-100 grid, but a 1-81 grid, arranged in nine rows of 9?

Challenge

Choose one of the shapes below, and try and find a way of finding the total of numbers in that shape anyway or anywhere on the grid. Or make up your own shape!

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**Investigation**

**Stars and crosses**

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## Investigation
### Stars and crosses

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